

# MATHEMATICS QUESTIONS BY TOPICS



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# MOTION AND FORCE

50 Multiple Choice Questions

# STUDENT BOOK

**Click here for the question index**

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## Mathematics Questions by Topics

### Motion and Force – Multiple Choice

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**Mathematics Questions by Topics**

Motion and Force

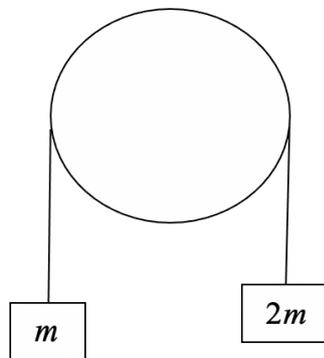
Question 1

Source: K22SM2Q14

**Question 1**

Two masses of mass  $m$  and  $2m$  kg are hanging vertically and connected by a light string which passes over a smooth pulley. In this situation the mass  $2m$  moves downwards with an acceleration of  $a \text{ ms}^{-2}$  and the tension in the string is  $T_1$  newtons. When an extra mass of  $3m$  is added to the mass  $m$ , it now moves down with the same acceleration of  $a \text{ ms}^{-2}$  and the tension in the string is  $T_2$  newtons. The ratio  $\frac{T_2}{T_1}$  is equal to.

- A.  $\frac{1}{3}$
- B. 1
- C. 2
- D. 3
- E. 4



**Mathematics Questions by Topics**

Motion and Force

Question 2

Source: K22SM2Q17

**Question 2**

A particle of mass  $m$  kg slides from rest down a smooth inclined plane, and travels a distance of  $S$  metres down the plane in a time of  $T_1$  seconds. Another particle of mass  $2m$  kg is placed on the same plane and travels a distance of  $2S$  metres down the plane in a time of  $T_2$ , seconds, then

**A.**  $T_2 = 4T_1$

**B.**  $T_2 = 2T_1$

**C.**  $T_2 = T_1$

**D.**  $T_2 = \frac{T_1}{2}$

**E.**  $T_2 = \sqrt{2}T_1$

**Mathematics Questions by Topics**

Motion and Force

Question 3

Source: K21SM2Q12

**Question 3**

A particle of mass 5 kg is on a rough horizontal plane. The particle is acted upon up by a force of  $T$  newtons acting at an angle of  $60^\circ$  to the plane. A frictional force of  $\frac{49\sqrt{3}}{3}$  newtons acting parallel to the plane, opposes the motion. Then if

- A.**  $T = \frac{98\sqrt{3} + 30}{3}$  the particle moves along the plane with an acceleration of  $1 \text{ ms}^{-2}$ .
- B.**  $T = \frac{98\sqrt{3} - 30}{3}$  the particle moves along the plane with an acceleration of  $1 \text{ ms}^{-2}$ .
- C.**  $T = \frac{98\sqrt{3} + 60}{3}$  the particle moves along the plane with an acceleration of  $2 \text{ ms}^{-2}$ .
- D.**  $T = \frac{98\sqrt{3} - 60}{3}$  the particle moves along the plane with an acceleration of  $2 \text{ ms}^{-2}$ .
- E.**  $T < \frac{98\sqrt{3}}{3}$  the particle does not move.

**Mathematics Questions by Topics**

Motion and Force

Question 4

Source: K21SM2Q15

**Question 4**

A particle of mass 2 kg, is moving so that its velocity vector at a time  $t$ , given by

$$\dot{\underline{r}}(t) = 4\sin^2(t)\underline{i} + 4\cos^2(t)\underline{j}, \text{ for } t \geq 0, \text{ given that } \underline{r}\left(\frac{\pi}{4}\right) = \frac{\pi}{2}(\underline{i} + \underline{j})$$

The change in momentum over  $\frac{\pi}{6} \leq t \leq \frac{\pi}{4}$ , is given by

- A.  $-2\underline{i} + 2\underline{j}$ .
- B.  $2\underline{i} - 2\underline{j}$ .
- C.  $\underline{i} - \underline{j}$
- D.  $-\underline{i} + \underline{j}$
- E.  $2\sqrt{2}$

## Mathematics Questions by Topics

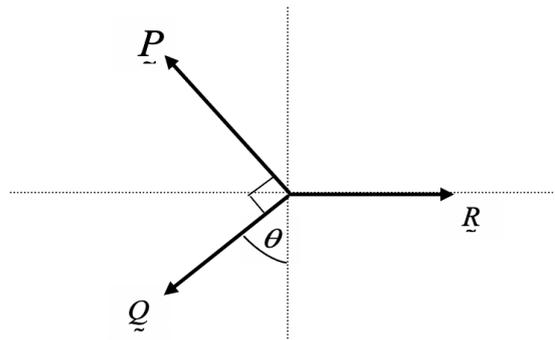
Motion and Force

Question 5

Source: K20SM2Q10

### Question 5

The following diagram shows a particle in equilibrium under the action of three concurrent coplanar forces  $\underline{P}$ ,  $\underline{Q}$  and  $\underline{R}$ . The forces,  $\underline{P}$ ,  $\underline{Q}$  and  $\underline{R}$  have magnitudes of  $P$ ,  $Q$  and  $R$  respectively.



Which one of the following statements is **not** correct?

- A.  $P \sec(\theta) = Q \operatorname{cosec}(\theta)$
- B.  $\cot(\theta) = \frac{P}{Q}$
- C.  $R = Q \sin(\theta) + P \cos(\theta)$
- D.  $R^2 = P^2 + Q^2$
- E.  $P + Q + R = 0$

**Mathematics Questions by Topics**

Motion and Force

Question 6

Source: K20SM2Q19

**Question 6**

A body is moving in a straight line. When its displacement is  $x$  metres from the origin at time  $t$  seconds,  $t = x \cos(2x)$ . The acceleration in  $\text{ms}^{-2}$  is given by

- A.  $\frac{-2 \sin(2x)}{\cos^3(2x)}$
- B.  $\frac{4(\sin(2x) + x \cos(2x))}{(\cos(2x) - 2x \sin(2x))^3}$
- C.  $\frac{4(\sin(2x) + x \cos(2x))}{(\cos(2x) - 2x \sin(2x))^2}$
- D.  $\frac{1}{\cos(2x) - 2x \sin(2x)}$
- E.  $-4(x \cos(2x) + 2 \sin(2x))$

## Mathematics Questions by Topics

Motion and Force

Question 7

Source: K20SM2Q20

### Question 7

A particle of mass  $m$  kg falls vertically downwards, from rest in a medium which offers air resistance equal to  $kv^2$  newtons, where  $v$   $\text{ms}^{-1}$  is its velocity at a time  $t$  seconds. After a time  $T$  seconds, its velocity is  $V$   $\text{ms}^{-1}$  and it has travelled a distance of  $D$  metres.

Which of the following is **false**?

A.  $m \frac{dv}{dt} = mg - kv^2$

B.  $D = \int_0^V \frac{mv}{mg - kv^2} dv$

C.  $V = \frac{D}{T}$

D.  $T = \int_0^V \frac{m}{mg - kv^2} dv$

E. Its limiting or terminal velocity is equal to  $\sqrt{\frac{mg}{k}}$   $\text{ms}^{-1}$ .

**Mathematics Questions by Topics**

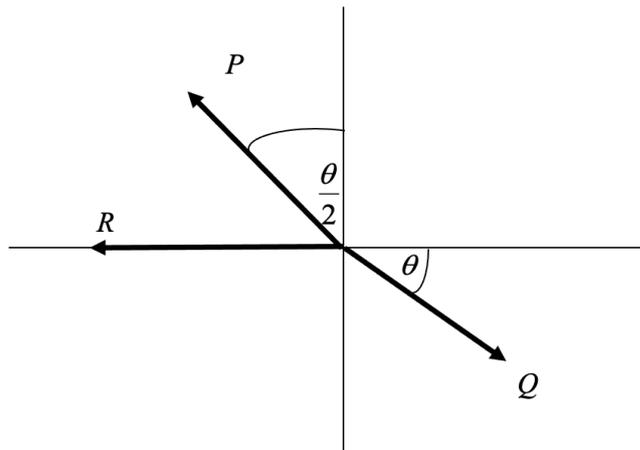
Motion and Force

Question 8

Source: K19SM2Q12

**Question 8**

Three coplanar forces of magnitudes  $P$ ,  $Q$  and  $R$  newtons act on a particle that is in equilibrium as shown in the diagram below.



Then,

- A.  $P \sin\left(\frac{\theta}{2}\right) = Q \cos(\theta)$
- B.  $P \cos\left(\frac{\theta}{2}\right) + R = Q \sin(\theta)$
- C.  $P = Q \sin\left(\frac{\theta}{2}\right)$
- D.  $P = 2Q \sin\left(\frac{\theta}{2}\right)$
- E.  $P + Q + R = 0$

**Mathematics Questions by Topics**

Motion and Force

Question 9

Source: K19SM2Q14

**Question 9**

A particle of mass 3 kg travels in a straight line with velocity  $v \text{ ms}^{-1}$  when its displacement is  $x$  metres, where  $v = \sqrt{4x^2 + 9}$ . The force in newtons acting on the particle when  $x = 2$  is

- A. 24
- B. 12
- C. 8
- D. 4
- E.  $\frac{24}{5}$

**Mathematics Questions by Topics**

Motion and Force

Question 10

Source: K19SM2Q17

**Question 10**

An object of mass 10 kg is initially at rest on a rough plane inclined at an angle of  $30^\circ$  to the horizontal. The object is pulled up the plane by a force of 75 N acting up and parallel to the plane. A frictional force of 11 N acting parallel to the plane, opposes the motion. After the pulling force has acted for 2 seconds, the magnitude of the momentum of the particle in  $\text{kg ms}^{-1}$  is closest to

- A. 10
- B. 20
- C. 30
- D. 40
- E. 50

## Mathematics Questions by Topics

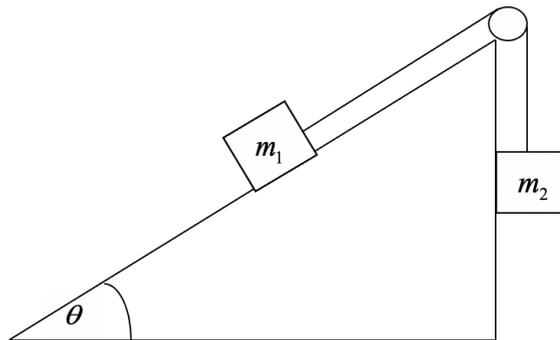
Motion and Force

Question 11

Source: K18SM2Q15

### Question 11

A particle of mass  $m_1$  kg is on a smooth plane, inclined at an angle of  $\theta$  to the horizontal. It is connected by a light string which passes around a smooth pulley to another mass of  $m_2$  kg hanging vertically, as shown in the diagram.



Then which of the following is **false**?

- A. If  $\theta = 30^\circ$  and  $\frac{m_2}{m_1} = \frac{1}{2}$  then the system is in equilibrium.
- B. If  $\theta = 30^\circ$  and  $\frac{m_2}{m_1} < \frac{1}{2}$  then the mass  $m_2$  moves upwards.
- C. If  $\theta = 45^\circ$  and  $\frac{m_2}{m_1} = \frac{\sqrt{2}}{2}$  then the system is in equilibrium.
- D. If  $\theta = 60^\circ$  and  $\frac{m_2}{m_1} = \frac{\sqrt{3}}{2}$  then the system is in equilibrium.
- E. If  $\theta = 60^\circ$  and  $\frac{m_2}{m_1} < \frac{\sqrt{3}}{2}$  then the mass  $m_2$  moves downwards.

**Mathematics Questions by Topics**

Motion and Force

Question 12

Source: K18SM2Q16

**Question 12**

A body is moving in a straight line. When its displacement is  $x$  metres from the origin at time  $t$  seconds, then  $t = e^{kx}$ , where  $k$  is a non-zero constant. The acceleration in  $\text{ms}^{-2}$  is given by

A.  $-e^{-kx}$

B.  $-\frac{e^{-kx}}{k^2}$

C.  $-\frac{e^{-2kx}}{k}$

D.  $-k$

E.  $e^{-2kx}$

**Mathematics Questions by Topics**

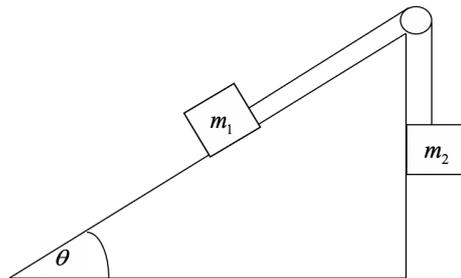
Motion and Force

Question 13

Source: K17SM2Q13

**Question 13**

A particle of mass  $m_1$  kg is on a smooth plane, inclined at an angle of  $\theta$  to the horizontal. It is connected by a light string which passes around a smooth pulley to another mass of  $m_2$  kg hanging vertically, as shown in the diagram.



Which of the following is **false**?

- A. The tension in the string is equal to  $\frac{m_1 m_2 (1 + \sin(\theta))}{m_1 + m_2}$  kg-wt.
- B. If  $m_2 > m_1 \sin(\theta)$  the mass  $m_2$  moves downwards with an acceleration  $\frac{g(m_2 - m_1 \sin(\theta))}{m_1 + m_2}$   $\text{ms}^{-2}$ .
- C. If  $m_2 = m_1 \sin(\theta)$  the masses remain at rest.
- D. If  $m_2 = 2m_1$  and  $\theta = 30^\circ$  the tension in the string is  $\frac{g}{2}$  newtons.
- E. If  $m_2 = 2m_1$  and  $\theta = 30^\circ$  the mass  $m_2$  moves downwards with an acceleration  $\frac{g}{2}$   $\text{ms}^{-2}$ .

**Mathematics Questions by Topics**

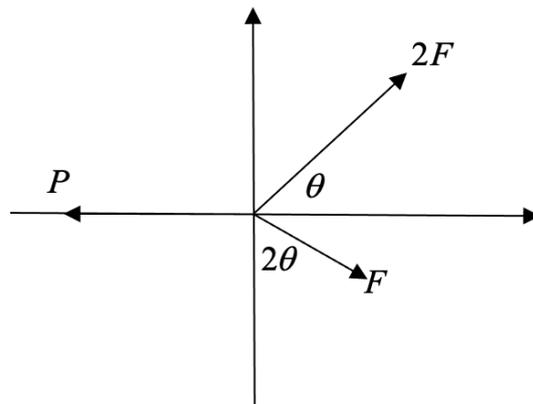
Motion and Force

Question 14

Source: K16SM2Q17

**Question 14**

A body is on a horizontal smooth plane and acted upon by three forces, with magnitudes and directions as shown in the diagram below.



The correct statement relating the magnitude of the forces and the angle  $\theta$  is

- A.  $P = 3F$
- B.  $P = 3F \sin(3\theta)$
- C.  $P = 3F \cos(3\theta)$
- D.  $P = 2F \sin(\theta) + F \cos(2\theta)$
- E.  $\theta = \sin^{-1}\left(\frac{\sqrt{3}-1}{2}\right)$

**Mathematics Questions by Topics**

Motion and Force

Question 15

Source: K15SM2Q15

**Question 15**

The position vector of a 2 kg moving particle is given by  $\underline{r}(t) = 4\sin(t)\underline{i} + \cos(2t)\underline{j}$  where the position is measured in metres and  $t \geq 0$  is the time in seconds. The maximum momentum in kg-m/s of the particle is

- A. 8
- B. 4
- C. 2
- D. 1
- E.  $2\sqrt{5}$

## Mathematics Questions by Topics

Motion and Force

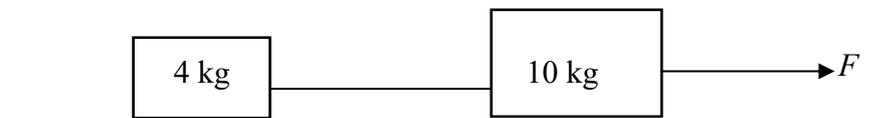
Question 16

Source: K15SM2Q16

### Question 16

Two boxes of masses 10 kg and 4 kg are connected by a light horizontal string and are on a horizontal table, as shown in the diagram below. The coefficient of friction between the 10 kg box and the table is 0.5. The contact between the 4 kg block and table is smooth. The 10 kg box is pulled by a force of  $F$ , parallel to the table.

Which of the following is **false**?



- A. If  $F = 50$  newtons, the boxes move with a constant acceleration equal to  $\frac{1}{14}$  m/s<sup>2</sup>
- B. If  $F = 49$  newtons, the boxes are on the point of moving.
- C. If  $F = 48$  newtons, the boxes move with constant velocity.
- D. If  $F = 47$  newtons the boxes remain at rest.
- E. If  $F = 46$  newtons

**Mathematics Questions by Topics**

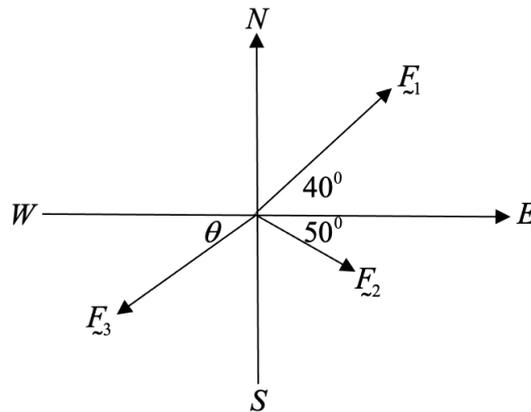
Motion and Force

Question 17

Source: K15SM2Q17

**Question 17**

A body is on a horizontal smooth plane and acted upon by three forces,  $F_1$ ,  $F_2$  and  $F_3$ . A north-south west-east framework is shown.



Given that  $|F_1| = 10$ ,  $|F_2| = 5$  and let  $F_3 = |F_3|$  and that the body moves in the north direction, then

- A.  $F_3 \cos(\theta) = 10.874$  and  $F_3 \sin(\theta) > 2.598$
- B.  $F_3 \cos(\theta) = 10.874$  and  $F_3 \sin(\theta) < 2.598$
- C.  $F_3 \sin(\theta) = 2.598$  and  $F_3 \sin(\theta) < 10.874$
- D.  $F_3 \sin(\theta) = 10.874$  and  $F_3 \cos(\theta) > 2.598$
- E.  $F_3 \sin(\theta) = 10.874$  and  $F_3 \cos(\theta) < 2.598$

**Mathematics Questions by Topics**

Motion and Force

Question 18

Source: K14SM2Q18

**Question 18**

A car is moving with constant acceleration has its speed reduced from  $3V \text{ ms}^{-1}$  to  $V \text{ ms}^{-1}$ , over a distance of  $D$  m when the driver applies the brakes. The car travels a further distance of  $S$  m until it comes to rest. The time  $T$  seconds represents the time when the driver applies the brakes until the car comes to rest. Then

- A.**  $D = 8S$  and  $T = \frac{2(D+S)}{3V}$
- B.**  $D = 4S$  and  $T = \frac{2(D+S)}{3V}$
- C.**  $D = 8S$  and  $T = \frac{S}{V}$
- D.**  $D = 4S$  and  $T = \frac{S}{V}$
- E.**  $D = 2S$  and  $T = \frac{D}{2V}$

**Mathematics Questions by Topics**

Motion and Force

Question 19

Source: K14SM2Q19

**Question 19**

A particle of mass  $M$  kg is on a horizontal table and is connected by a light string to a particle of mass 2 kg hanging vertically at the edge of the table. The coefficient of friction between the table and the mass  $M$  is equal to  $\frac{1}{3}$ . Then if

- A.**  $M > 6$  both masses move with constant acceleration.
- B.**  $0 < M < 6$  both masses move with constant acceleration.
- C.**  $0 < M \leq 6$  the system is in limiting equilibrium.
- D.**  $M > 6$  both masses move with constant velocity.
- E.**  $0 < M < 6$  both masses move with constant velocity.

**Mathematics Questions by Topic**

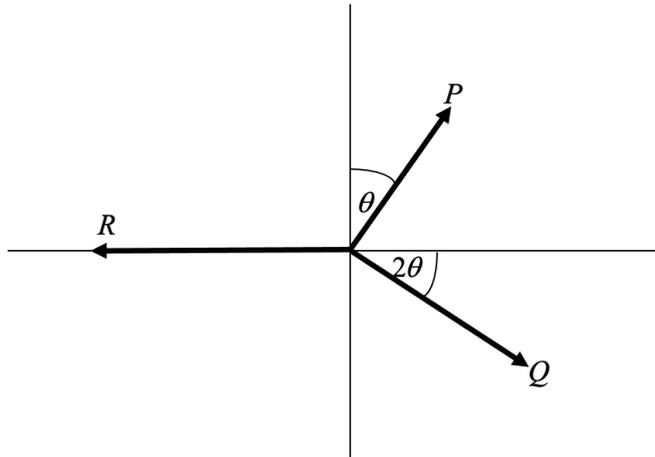
Motion and Force

Question 20

Source: K14SM2Q20

**Question 20**

Three coplanar forces of magnitudes  $P$ ,  $Q$  and  $R$  newtons act on a particle that is in equilibrium as shown in the diagram below.



Then,

- A.  $Q = R$  and  $P = 2R \sin(\theta)$
- B.  $Q = R$  and  $P = 2R \cos(\theta)$
- C.  $Q = 2P$  and  $R = P \sin(\theta)$
- D.  $P = Q$  and  $R = 2P \sin(\theta)$
- E.  $P + Q + R = 0$

**Mathematics Questions by Topics**

Motion and Force

Question 21

Source: K14SM2Q21

**Question 21**

A particle of mass 10 kg travels in a straight line with velocity  $v \text{ ms}^{-1}$  when its displacement is  $x$  metres, where  $v = 2 \log_e(\sqrt{x^2 + 1} + x)$  for  $x \geq 0$ . The maximum force in newtons acting on the particle is closest to

- A. 1.5
- B. 2.7
- C. 20
- D. 24
- E. 26.5

**Mathematics Questions by Topics**

Motion and Force

Question 22

Source: K13SM2Q11

**Question 22**

A particle is acted upon by two forces. One has a magnitude of  $\sqrt{2}b$  newtons and acts in the direction  $S45^\circ E$ , the other has a magnitude of  $\sqrt{2}c$  newtons and acts in the direction  $N45^\circ E$ , where  $b$  and  $c$  are non-zero real positive constants. The magnitude of the resultant force is equal to

A.  $\sqrt{2}(b+c)$

B.  $\frac{\sqrt{2}}{2}(b+c)$

C.  $2\sqrt{2(b^2+c^2)}$

D.  $\sqrt{2(b^2+c^2)}$

E.  $2\sqrt{b^2+c^2}$

**Mathematics Questions by Topics**

Motion and Force

Question 23

Source: K13SM2Q12

**Question 23**

A car of mass  $m$  kg is travelling on a level roadway. The engine exerts a constant propulsive force of  $F$  newtons and the total resistance to the motion of the car is  $kv$  newtons, where  $k$  is positive constant and  $v$  is its speed in m/s. The car moves from rest, and travels a distance of  $D$  metres until it obtains a speed of  $V$  m/s, in a time of  $T$  seconds.



Five students stated some relationships between the constants,  $m$ ,  $V$ ,  $k$ ,  $F$ ,  $D$  and  $T$ .

Alan stated that  $mV = (F - kV)T$       Ben stated that  $2mD = (F - kV)T^2$

Colin stated that  $\frac{1}{2}mV^2 = (F - kV)D$       David stated that  $D = \int_0^V \frac{mv}{F - kv} dv$

Edward stated that  $T = \int_0^V \frac{m}{F - kv} dv$

Then

- A. Alan, Ben and Colin are all correct.
- B. Alan and Colin are both correct.
- C. Only Colin is correct.
- D. David and Edward are both correct.
- E. Only Edward is correct.

**Mathematics Questions by Topics**

Motion and Force

Question 24

Source: K13SM2Q13

**Question 24**

A girl of mass 50 kg is standing in a lift. The reaction of the lift floor on the girl is equal to 60 kg-wt. Then the lift is moving

- A. with constant speed.
- B. down with an acceleration equal to  $1.96 \text{ ms}^{-2}$ .
- C. up with an acceleration equal to  $1.96 \text{ ms}^{-2}$ .
- D. down with an acceleration equal to  $0.2 \text{ ms}^{-2}$ .
- E. up with an acceleration equal to  $0.2 \text{ ms}^{-2}$ .

## Mathematics Questions by Topics

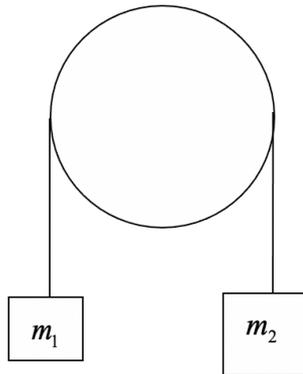
Motion and Force

Question 25

Source: K13SM2Q21

### Question 25

A light inextensible string passes over a smooth pulley, with particles of masses  $m_1$  and  $m_2$  kg, attached to each end of the string as shown in the diagram.



Which of the following is **false**?

- A. If  $m_2 = 2m_1$  the mass  $m_2$  moves downwards with an acceleration  $\frac{g}{2} \text{ ms}^{-2}$ .
- B. If  $m_1 = m_2 = m$  the tension in the string is equal to  $mg$  newtons.
- C. If  $m_1 = m_2$  both masses remain at rest.
- D. If  $m_2 > m_1$  the mass  $m_2$  moves downwards with an acceleration  $\frac{(m_2 - m_1)g}{m_1 + m_2} \text{ ms}^{-2}$ .
- E. If  $m_1 \neq m_2$  the tension in the string is equal to  $\frac{2m_1m_2}{m_1 + m_2}$  kg-wt.

**Mathematics Questions by Topics**

Motion and Force

Question 26

Source: K13SM2Q22

**Question 26**

A particle of mass  $m$  kg is acted upon by a variable force, so that its velocity  $v$  m/s when the particle is  $x$  m from the origin is given by  $v = e^{cx}$ , where  $c$  is a non-zero real constant. The force acting on the particle when  $x = \frac{1}{c}$ , in newtons, is

- A.  $mc^2$
- B.  $mec$
- C.  $me$
- D.  $me^2$
- E.  $mce^2$

**Mathematics Questions by Topics**

Motion and Force

Question 27

Source: K12SM2Q14

**Question 27**

A body moves in a straight line such that its velocity  $v \text{ ms}^{-1}$  is given by  $v(x) = e^{2x} - e^{-2x}$ , where  $x$  metres is its displacement from the origin. The acceleration of the body in  $\text{ms}^{-2}$  is given by

- A.  $4(e^{4x} - e^{-4x})$
- B.  $2(e^{4x} - e^{-4x})$
- C.  $e^{4x} - e^{-4x}$
- D.  $2(e^{2x} + e^{-2x})$
- E.  $-4x$

**Mathematics Questions by Topics**

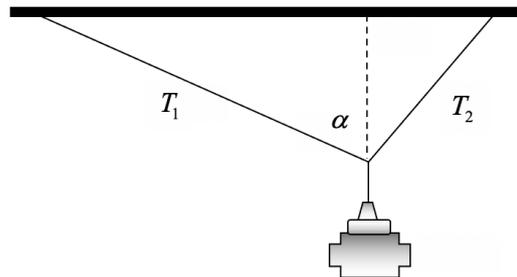
Motion and Force

Question 28

Source: K12SM2Q17

**Question 28**

An engine weighing 5 kg is suspended by two ropes at right angles to one another, which support tensions of  $T_1$  and  $T_2$  newtons. The rope supporting a tension of  $T_1$  makes an angle of  $\alpha$  to the vertical as shown in the diagram below.



Then,

- A.  $T_1 = 5 \sin(\alpha)$  and  $T_2 = 5 \cos(\alpha)$
- B.  $T_1 = 5 \cos(\alpha)$  and  $T_2 = 5 \sin(\alpha)$
- C.  $T_1 = 5 \tan(\alpha)$  and  $T_2 = \frac{5}{\tan(\alpha)}$
- D.  $T_1 = 49 \sin(\alpha)$  and  $T_2 = 49 \cos(\alpha)$
- E.  $T_1 = 49 \cos(\alpha)$  and  $T_2 = 49 \sin(\alpha)$

**Mathematics Questions by Topics**

Motion and Force

Question 29

Source: K12SM2Q20

**Question 29**

A constant force of 10 newtons acts on a mass of 5 kg initially moving at  $1 \text{ ms}^{-1}$ . After the mass has moved a distance of 20 metres, the magnitude of the momentum in  $\text{kgms}^{-1}$ , is equal to

- A. 9
- B. 10
- C. 40
- D. 45
- E. 50

**Mathematics Questions by Topics**

Motion and Force

Question 30

Source: K11SM2Q15

**Question 30**

A hot air balloon is accelerating upwards with an acceleration of  $1 \text{ m/s}^2$ . At a particular instant it is 250 metres above ground level and rising upwards with a speed of  $3 \text{ m/s}$ . A small stone falls from the balloon to the ground. Assuming air resistance is negligible, the time taken, for the stone to hit the ground in seconds, is closest to

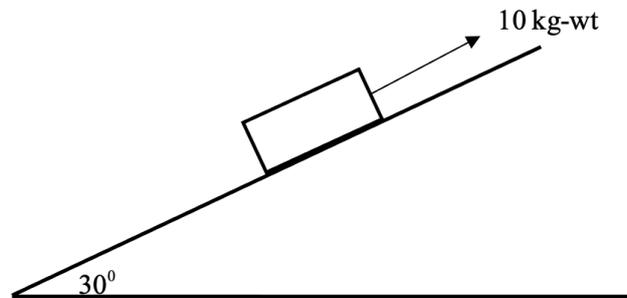
- A. 7.89
- B. 7.54
- C. 7.46
- D. 7.20
- E. 7.14

**Mathematics Questions by Topics**

Motion and Force

Question 31

Source: K11SM2Q17

**Question 31**

A box of mass 10 kg is at rest on a plane inclined at angle of  $30^\circ$  to the horizontal. A force of magnitude 10 kg-wt acting up and parallel to the plane is applied to the box.

For equilibrium to be maintained, the co-efficient of friction between the box and the plane must be

- A. at least  $\frac{\sqrt{3}}{3}$
- B. less than  $\frac{\sqrt{3}}{3}$
- C. at least  $\frac{g-2}{g\sqrt{3}}$
- D. less than  $\frac{g-2}{g\sqrt{3}}$
- E. at least  $5g\sqrt{3}$

**Mathematics Questions by Topics**

Motion and Force

Question 32

Source: K11SM2Q18

**Question 32**

A body of mass  $m$  kg moves in a straight line, its velocity is  $v$   $\text{ms}^{-1}$  at a time  $t$  seconds. The force acting on the body is  $f(t)$  newtons.

Given that  $v = v_1$  when  $t = t_1$  and  $v = v_2$  when  $t = t_2$ , it follows that

- A.  $mv_2 - mv_1 = f(t_2) - f(t_1)$
- B.  $mv_2 - mv_1 = \int_{t_1}^{t_2} f(t) dt$
- C.  $v_2 - v_1 = m \int_{t_1}^{t_2} f(t) dt$
- D.  $\frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2 = f(t_2) - f(t_1)$
- E.  $\frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2 = \int_{t_1}^{t_2} f(t) dt$

**Mathematics Questions by Topics**

Motion and Force

Question 33

Source: K11SM2Q19

**Question 33**

A car of mass  $m$  kg is travelling on a level roadway. The engine exerts a constant propulsive force of  $F$  newtons and the total resistance to the motion of the car is  $kv^3$  newtons, where  $k$  is positive constant and  $v$  is its speed in m/s. The car moves from rest, the distance travelled in metres until it obtains a speed of  $V$ , is given by



- A.  $\frac{V^2}{2(F - kV^3)}$
- B.  $\frac{mV^2}{2(F - kV^3)}$
- C.  $\frac{m}{2} \int_0^V \frac{v^2}{F - kv^3} dv$
- D.  $\int_0^V \frac{mv}{F - kv^3} dv$
- E.  $\int_0^V \frac{v}{F - kv^3} dv$

**Mathematics Questions by Topics**

Motion and Force

Question 34

Source: K10SM2Q13

**Question 34**

A particle of mass 5 kg, initially at rest is acted upon by two forces. One force has a magnitude of  $5\sqrt{2}$  newtons acting in the north-west direction, the other force has magnitude of 10 newtons acting in the east direction. After two seconds, the magnitude of the momentum of the particle in  $\text{kg ms}^{-1}$  is equal to

- A.  $50\sqrt{2}$
- B.  $25\sqrt{2}$
- C.  $10\sqrt{2}$
- D.  $2(2 - \sqrt{2})$
- E.  $2\sqrt{2}$

**Mathematics Questions by Topics**

Motion and Force

Question 35

Source: K10SM2Q17

**Question 35**

A body of mass  $m$  kg moves in a straight line. When its displacement is  $x$  m from the origin, its velocity is  $v$  ms<sup>-1</sup> at a time  $t$  seconds. The force acting on the body is  $mf(x)$  newtons. Given that  $v = v_0$  when  $x = x_0$  and  $v = v_1$  when  $x = x_1$ , it follows that

A.  $\frac{1}{2}mv_1^2 - \frac{1}{2}mv_0^2 = m[f(x_1) - f(x_0)]$

B.  $\frac{1}{2}mv_1^2 - \frac{1}{2}mv_0^2 = m \int_{x_0}^{x_1} f(x) dx$

C.  $v_1 - v_0 = [f(x_1) - f(x_0)]$

D.  $v_1 - v_0 = \int_{x_0}^{x_1} f(x) dx$

E.  $v_1 = \sqrt{v_0^2 + m \int_{x_0}^{x_1} f(x) dx}$

**Mathematics Questions by Topics**

Motion and Force

Question 36

Source: K10SM2Q18

**Question 36**

An object of mass  $m$  kg is projected downwards from a point  $P$ , with an initial speed of  $U$  m/s. The object falls under the influence of gravity in a medium which offers resistance proportional to the velocity. Take the initial position as  $y = 0$  and downwards as the positive direction. If  $k$  is a positive constant, which of the following most accurately reflects the situation ?

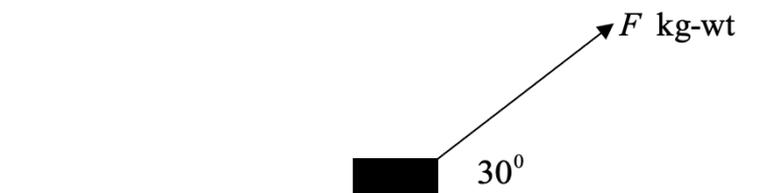
- A.  $\ddot{y} - k\dot{y} = mg$     $y(0) = 0$     $\dot{y}(0) = U$
- B.  $\ddot{y} - k\dot{y} = g$     $y(0) = 0$     $\dot{y}(0) = -U$
- C.  $\ddot{y} + k\dot{y} = mg$     $y(0) = 0$     $\dot{y}(0) = U$
- D.  $\ddot{y} + k\dot{y} = mg$     $y(0) = 0$     $\dot{y}(0) = -U$
- E.  $\ddot{y} + k\dot{y} = g$     $y(0) = 0$     $\dot{y}(0) = U$

**Mathematics Questions by Topics**

Motion and Force

Question 37

Source: K10SM2Q21

**Question 37**

A box of mass 3 kg is on a horizontal plane. A force of magnitude  $F$  kg-wt acting at an angle of  $30^\circ$  to the horizontal is applied to the box.

The coefficient of friction between the box and the plane is  $\frac{\sqrt{3}}{2}$ .

Which of the following is true?

- A. If  $F < 2g$  the box is not on the point of moving.
- B. If  $F < 2g$  the box moves with constant velocity.
- C. If  $F = 2$  the box moves with constant acceleration.
- D. If  $F > 2$  the box moves with constant velocity.
- E. If  $F > 2$  the box moves with constant acceleration.

**Mathematics Questions by Topics**

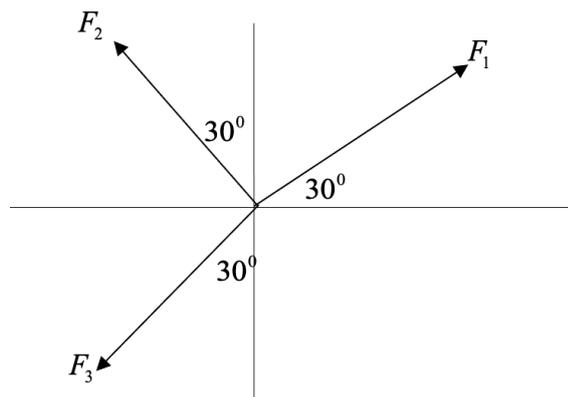
Motion and Force

Question 38

Source: K9SM2Q11

**Question 38**

Three co-planar forces,  $F_1, F_2, F_3$  act on a particle in equilibrium as shown in the diagram below



It follows that

- A.**  $F_1 = F_2 = F_3$
- B.**  $3F_2 = \sqrt{3}F_1$  and  $F_2 = \frac{2}{3}F_3$
- C.**  $F_1 = \sqrt{3}F_2$  and  $F_3 = 2F_2$
- D.**  $\sqrt{3}F_1 = 3F_2$  and  $F_2 = \frac{3}{2}F_3$
- E.**  $\sqrt{3}F_3 = 3F_2$  and  $F_1 = \frac{3}{2}F_3$

**Mathematics Questions by Topics**

Motion and Force

Question 39

Source: K9SM2Q18

**Question 39**

A parcel of mass 2 kg, is at rest on a rough horizontal table. The coefficient of friction between the parcel and the table is 0.25. A constant horizontal force of 10 newtons is applied to the parcel. Two seconds later the magnitude of the momentum of the parcel in kg m/s is equal to

- A. 5.1
- B. 10
- C. 10.2
- D. 20
- E. 186.2

## Mathematics Questions by Topics

Motion and Force

Question 40

Source: K9SM2Q21

### Question 40

A sand bag of mass 9 kg is dropped from a stationary hot-air balloon, which is 150 metres above the ground. Which of the following is true?

- A. The sand bag hits the ground after 5.48 seconds, with a speed of 54.78m/s.
- B. The sand bag hits the ground after 5.48 seconds, with a speed of 53.68 m/s.
- C. The sand bag hits the ground after 5.53 seconds, with a speed of 55.33m/s.
- D. The sand bag hits the ground after 5.53 seconds, with a speed of 54.22m/s.
- E. The sand bag hits the ground after 5.68 seconds with a speed of 50m/s.

**Mathematics Questions by Topics**

Motion and Force

Question 41

Source: K9SM2Q22

**Question 41**

Two boxes of masses 2 kg and 3 kg are connected by a light horizontal string and are on a horizontal table, as shown in the diagram below. The coefficient of friction between both boxes and the table is  $\frac{1}{7}$ . The 3 kg box is pulled by a force of  $F$ , parallel to the table.

Which of the following is true?



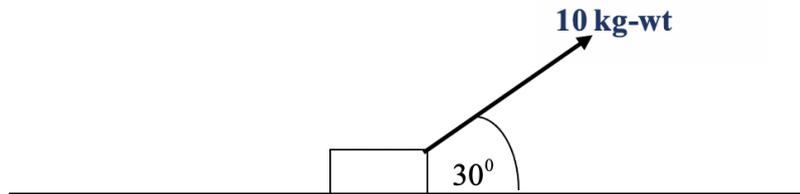
- A. If  $F > 7$  newtons, the boxes move with constant acceleration.
- B. If  $5 < F < 7$  newtons, the boxes are on the point of moving.
- C. If  $F = 7$  newtons, the boxes move with constant velocity.
- D. If  $F > 7$  kg-wt, the boxes move with constant velocity.
- E. If  $F = 7$  kg-wt, the boxes are not on the point of moving.

**Mathematics Questions by Topics**

Motion and Force

Question 42

Source: K8SM2Q13

**Question 42**

A box of mass 20 kg is at rest on a horizontal plane. A force of magnitude 10 kg-wt acting at an angle of  $30^\circ$  to the horizontal is applied to the block. For equilibrium to be maintained, the coefficient of friction between the box and the plane must be

- A. at least  $\frac{\sqrt{3}}{3}$
- B. less than  $\frac{\sqrt{3}}{3}$
- C. at least  $\frac{\sqrt{3}}{4}$
- D. at least  $\frac{\sqrt{3}}{4g}$
- E. less than  $\frac{\sqrt{3}}{4g}$

**Mathematics Questions by Topics**

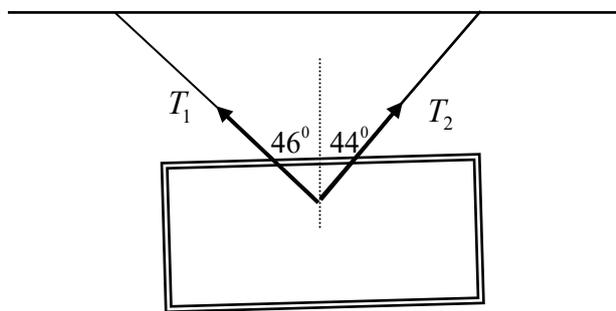
Motion and Force

Question 43

Source: K8SM2Q14

**Question 43**

A painting of mass one kilogram is to be hung on a wall using two light strings. Unfortunately the painting is not quite horizontal. One string makes an angle of  $46^\circ$  with the vertical and has a tension of magnitude  $T_1$  newtons. The other string makes an angle of  $44^\circ$  with the vertical and has a tension of magnitude  $T_2$  newtons, as shown in the diagram below.



Which of the following is true?

- A.  $\frac{T_1}{T_2} = \tan(44^\circ)$
- B.  $\frac{T_1}{T_2} = \tan(46^\circ)$
- C.  $T_1 + T_2 = g$
- D.  $T_1^2 + T_2^2 = g^2$
- E.  $T_1 = T_2$

**Mathematics Questions by Topics**

Motion and Force

Question 44

Source: K8SM2Q18

**Question 44**

A hot air balloon is accelerating vertically upwards with an acceleration of  $1 \text{ m/s}^2$ . A stone is dropped from the balloon when it is  $h$  metres above the ground. The stone strikes the ground 8 seconds later. Assuming the air resistance is negligible, the value of  $h$  is closest to

- A. 282.
- B. 290.
- C. 314.
- D. 322.
- E. 346.

**Mathematics Questions by Topics**

Motion and Force

Question 45

Source: K7SM2Q16

**Question 45**

A particle travels in a straight line with velocity  $v$  at a time  $t$  and its displacement is  $x$ .

If  $v^2 = 9x$  for  $x > 0$ , then the acceleration of the particle is given by

- A.  $\frac{2x}{3}$
- B. 4.5
- C.  $2\sqrt{x^3}$
- D.  $6x^2$
- E.  $\frac{3}{2\sqrt{x}}$

**Mathematics Questions by Topics**

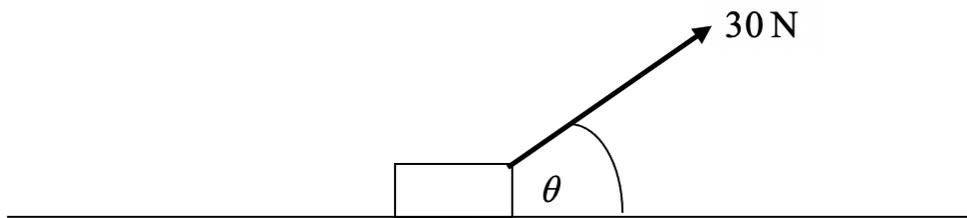
Motion and Force

Question 46

Source: K7SM2Q17

**Question 46**

A box of mass 10 kg is on a horizontal plane. A rope makes an angle of  $\theta^\circ$  with the horizontal and exerts a tension of 30 newtons.



If the coefficient of friction between the block and the surface is 0.2, which one of the following values of  $\theta$  produces the largest acceleration of the block?

- A.  $\theta = 0$
- B.  $\theta = 5$
- C.  $\theta = 10$
- D.  $\theta = 15$
- E.  $\theta = 20$

**Mathematics Questions by Topics**

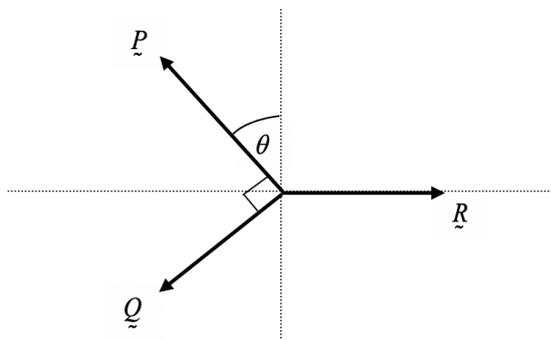
Motion and Force

Question 47

Source: K7SM2Q18

**Question 47**

The following diagram shows a particle in equilibrium under the action of three concurrent coplanar forces  $\vec{P}$ ,  $\vec{Q}$  and  $\vec{R}$ . The forces  $\vec{P}$ ,  $\vec{Q}$  and  $\vec{R}$  have magnitudes of  $P$ ,  $Q$  and  $R$  respectively. Which one of the following statements is **not** correct?



- A.**  $P \operatorname{cosec}(\theta) = Q \sec(\theta)$
- B.**  $R^2 = P^2 + Q^2$
- C.**  $R = P \sin(\theta) + Q \cos(\theta)$
- D.**  $\cot(\theta) = \frac{P}{Q}$
- E.**  $\vec{P} + \vec{Q} + \vec{R} = \vec{0}$

**Mathematics Questions by Topics**

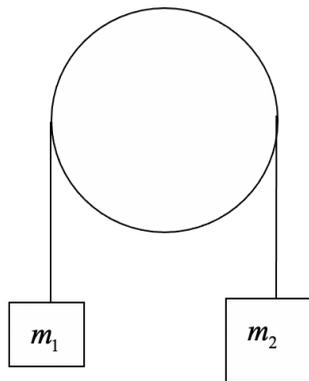
Motion and Force

Question 48

Source: K7SM2Q21

**Question 48**

A light inextensible string passes over a smooth pulley. Particles of masses  $m_1$  and  $m_2$  are attached to each end of the string as shown in the diagram.



If the mass  $m_2$  accelerates downwards at  $\frac{g}{5} \text{ m/s}^2$ , then the ratio  $\frac{m_2}{m_1}$  is equal to

- A. 1
- B.  $\frac{3}{2}$
- C.  $\frac{2}{3}$
- D. 5
- E.  $\frac{5}{4}$

**Mathematics Questions by Topics**

Motion and Force

Question 49

Source: K5SM1Q25

**Question 49**

A suitcase of mass 12 kilograms rests on a rough, level ground. The suitcase is pulled with a force of magnitude  $P$  newtons acting at an angle of  $30^\circ$  to the horizontal. The suitcase is just on the point of sliding along the ground. If the coefficient of friction between the suitcase and the plane is 0.25, then  $P$  is closest to

- A. 58.8
- B. 29.67
- C. 39.67
- D. 3.03
- E. 33.95

**Mathematics Questions by Topics**

Motion and Force

Question 50

Source: K5SM1Q29

**Question 50**

A block of mass  $m$  kg is lying on a smooth horizontal table and is joined by a light inextensible string to a another block of mass of  $2m$  kg hanging vertically. This string passes over a smooth pulley at the edge of the table. When the system is released from rest, the acceleration of the blocks in  $\text{m/s}^2$  is given by

- A.  $\frac{2}{3}$
- B.  $\frac{2g}{3}$
- C. 1
- D.  $2g$
- E.  $g$

End of  
**MATHEMATICS QUESTIONS BY TOPICS**  
**MOTION AND FORCE**  
50 Multiple Choice Questions